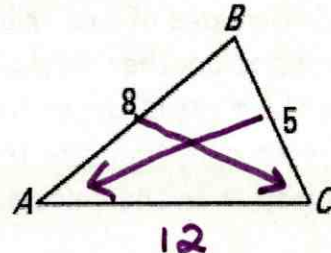
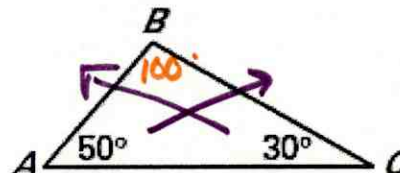
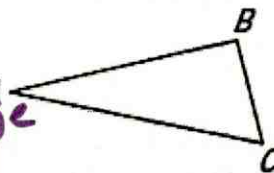


5.5

Use Inequalities in Triangles

| Vocabulary | Definition | Example |
|-----------------------------|--|---|
| THEOREM 5.10 | If one side of a triangle is longer than another side, then the angle opposite the longer side is larger than the angle opposite the shorter side. |  <p> $8 \quad 5$ $AB > BC$, so $m\angle C > m\angle A$. </p> |
| THEOREM 5.11 | <p><i>angle</i></p> If one of a triangle is larger than another angle, then the side opposite the larger angle is longer than the side opposite the smaller angle. |  <p> $50^\circ \quad 30^\circ$ $m\angle A > m\angle C$, so $\overline{BC} > \overline{AB}$. </p> <p><i>AC is the longest side</i></p> |
| TRIANGLE INEQUALITY THEOREM | The sum of the lengths of any two sides of a triangle is greater than the length of the third side. | <p><i>small + small > large</i></p> <div style="border: 1px solid black; padding: 5px; display: inline-block;"> $\overline{AB} + \overline{BC} > \overline{AC}$ </div> <p> $\overline{AC} + \overline{BC} > \overline{AB}$ $\overline{AB} + \overline{AC} > \overline{BC}$ </p>  <p>can you construct a Δ w/ side lengths of 2, 8, 9?</p> <p> $2 + 8 > 9$ $10 > 9$ <i>yes</i> </p> |

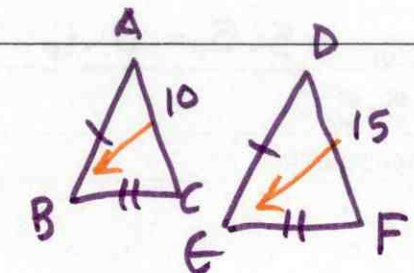
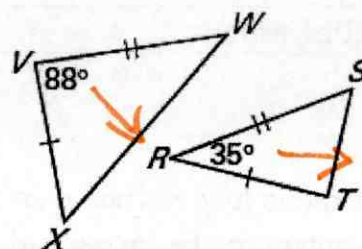
5, 5, 10
 $5 + 5 > 10$
 $10 > 10$ NO

12, 18, 15
 $12 + 15 > 18$
 $27 > 18$ *yes*

5.6

HINGE
THEOREM

If two sides of one triangle are congruent to two sides of another triangle, and the included angle of the first is larger than the included angle of the second, then the third side of the first is longer than the third side of the second.

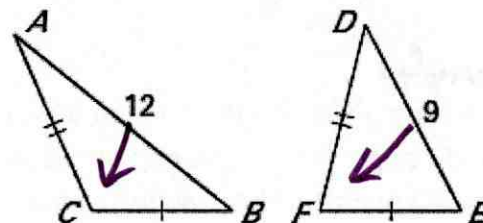


$$88 > 35 \quad 15 > 10$$

$$WX > \underline{ST} \quad \angle E > \angle B$$

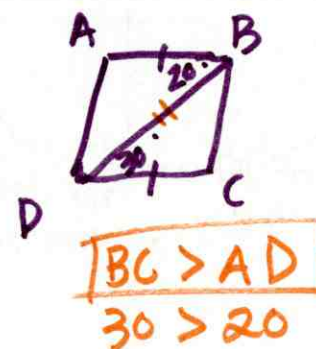
CONVERSE of
the HINGE
THEOREM

If two sides of one triangle are congruent to two sides of another triangle, and the third side of the first is longer than the third side of the second, then the included angle of the first is larger than the included angle of the second.



$$m\angle C > m\angle F$$

$$12 > 9$$



$$\boxed{BC > AD}$$

$$30 > 20$$

Describe possible side lengths of third side of a Δ

given 2 sides

$$a - b < x < a + b$$

a is the larger #
b is the smaller #

$$\begin{matrix} b & a \\ 3, & 5, & x \end{matrix}$$

$$5 - 3 < x < 5 + 3$$

$$\boxed{2 < x < 8}$$

$$12, 7, x$$

$$12 - 7 < x < 12 + 7$$

$$\boxed{5 < x < 19}$$

$$20, 4, x - 5$$

$$20 - 4 < x - 5 < 20 + 4$$

$$16 < x - 5 < 24$$

$$\begin{array}{r} 16 < x - 5 & x - 5 < 24 \\ + 5 & + 5 \\ \hline 21 < x & x < 29 \end{array}$$

$$\boxed{21 < x < 29}$$