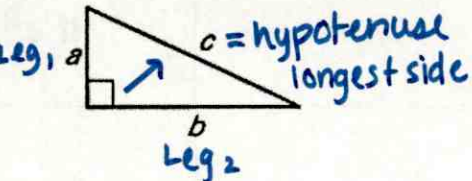
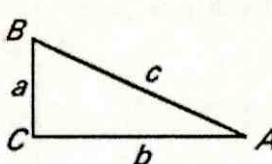


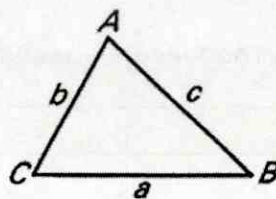
Apply Pythagorean Theorem and Use the Converse

7.1

Vocabulary	Definition	Example																				
<p>THEOREM 7.1 PYTHAGOREAN THEOREM</p>	<p>In a right triangle, the square of the length of the hypotenuse is equal to the sum of the squares of the lengths of the legs.</p>	<div style="text-align: right;"> <math display="block">c^2 = a^2 + b^2 \cdot c = \sqrt{a^2 + b^2}</math> </div>  <div style="text-align: right; color: red;"> <math display="block">a^2 = c^2 - b^2</math> <math display="block">b^2 = c^2 - a^2</math> </div>																				
<p>PYTHAGOREAN TRIPLE</p> <p>7.2</p>	<p>A Pythagorean triple is a set of three positive integers a, b, and c that satisfy the equation <math>c^2 = a^2 + b^2</math>.</p>	<table border="1" style="width: 100%; border-collapse: collapse; text-align: center;"> <tr style="border: 2px solid red;"> <td><b>3, 4, 5</b></td> <td><b>5, 12, 13</b></td> <td><b>8, 15, 17</b></td> <td><b>7, 24, 25</b></td> </tr> <tr> <td>6, 8, 10</td> <td>10, 24, 26</td> <td>16, 30, 34</td> <td>14, 48, 50</td> </tr> <tr> <td>9, 12, 15</td> <td>15, 36, 39</td> <td>24, 45, 51</td> <td>21, 72, 75</td> </tr> <tr> <td>30, 40, 50</td> <td>50, 120, 130</td> <td>80, 150, 170</td> <td>70, 240, 250</td> </tr> <tr> <td>3x, 4x, 5x</td> <td>5x, 12x, 13x</td> <td>8x, 15x, 17x</td> <td>7x, 24x, 25x</td> </tr> </table>	<b>3, 4, 5</b>	<b>5, 12, 13</b>	<b>8, 15, 17</b>	<b>7, 24, 25</b>	6, 8, 10	10, 24, 26	16, 30, 34	14, 48, 50	9, 12, 15	15, 36, 39	24, 45, 51	21, 72, 75	30, 40, 50	50, 120, 130	80, 150, 170	70, 240, 250	3x, 4x, 5x	5x, 12x, 13x	8x, 15x, 17x	7x, 24x, 25x
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<p>THEOREM 7.2 CONVERSE of PYTHAGOREAN THEOREM</p>	<p>If the square of the length of the longest side of a triangle is equal to the sum of the squares of the other two sides, then the triangle is a <u>right</u> triangle.</p>	 <div style="text-align: right; color: red;"> <math display="block">c^2 = a^2 + b^2</math> <p>↓ longest side</p> </div> <p>If <math>c^2 = a^2 + b^2</math>, then <math>\triangle ABC</math> is a <u>right</u> triangle.</p>																				

**THEOREM 7.3**

If the square of the length of the longest side of a triangle is less than the sum of the squares of the other two sides, then the triangle is an acute triangle.

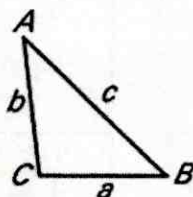


$$c^2 < a^2 + b^2$$

If  $c^2 < a^2 + b^2$ , then the triangle ABC is acute.

**THEOREM 7.4**

If the square of the length of the longest side of a triangle is greater than the sum of the squares of the other two sides, then the triangle is an obtuse triangle.

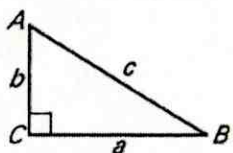


$$c^2 > a^2 + b^2$$

If  $c^2 > a^2 + b^2$ , then the triangle ABC is obtuse.

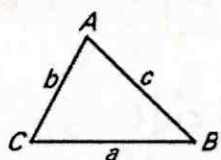
**METHODS FOR CLASSIFYING A TRIANGLE BY ANGLES USING ITS SIDE LENGTHS**

**Theorem 7.2**



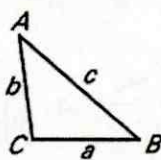
If  $c^2 = a^2 + b^2$ , then  $m\angle C = 90^\circ$  and  $\triangle ABC$  is a right triangle.

**Theorem 7.3**



If  $c^2 < a^2 + b^2$ , then  $m\angle C < 90^\circ$  and  $\triangle ABC$  is an acute triangle.

**Theorem 7.4**



If  $c^2 > a^2 + b^2$ , then  $m\angle C > 90^\circ$  and  $\triangle ABC$  is an obtuse triangle.

<p>6, 7, 9</p> $9^2 < 6^2 + 7^2$ <p>81      36 + 49</p> <p style="text-align: center;">85</p> <p>Acute</p>	<p>10, 4, 8</p> $10^2 > 4^2 + 8^2$ <p>100    16 + 64</p> <p style="text-align: center;">80</p> <p>obtuse</p>	<p>3, 5, <math>\sqrt{34}</math></p> $(\sqrt{34})^2 = 3^2 + 5^2$ <p>34            9 + 25</p> <p style="text-align: center;">34</p> <p>Right</p>
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