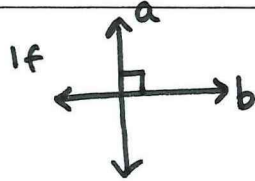
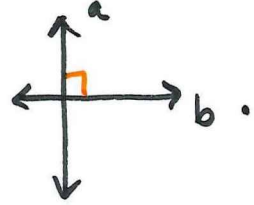
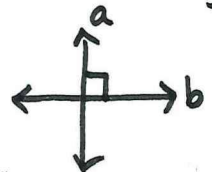


Analyze Conditional Statements

| Vocabulary | Definition | Symbol | Example |
|-----------------------|---|--|--|
| CONDITIONAL STATEMENT | A logical statement that has two parts, a hypothesis and a conclusion. | | All dogs are mammals . |
| IF-THEN FORM | A form of a conditional statements in which the "if" part ^{contains} follows the hypothesis and the "then" part contains the conclusion. | $P \rightarrow Q$ $\rightarrow = \text{then}$ | ^P <u>If an animal is a dog, then it is</u> <u>a mammal.</u> _Q " If P, then Q ." True Valid |
| HYPOTHESIS | A hypothesis is the "if" part of a conditional statement. | P | P = an animal is a dog |
| CONCLUSION | A conclusion is the "then" part of a conditional statement. | Q | Q = it is a mammal . |

| | | | |
|-----------------------|---|---|---|
| <p>NEGATION</p> | <p>The negation of a statement is the opposite of the original statement.</p> | <p>\sim not</p> | <p>I like blue. P I do not like blue. $\sim P$</p> |
| <p>CONVERSE</p> | <p>The converse of a conditional statement is formed by <u>switching the hypothesis and the conclusion.</u></p> | <p>$Q \rightarrow P$</p> | <p>If <u>an animal is a dog</u>, then <u>it's a mammal</u>. P Q If <u>an animal is a mammal</u>, then <u>it is a dog</u>. Q P False invalid</p> |
| <p>INVERSE</p> | <p>The inverse of a conditional statement is formed by <u>negating both the hypothesis and conclusion.</u> negate the conditional $\sim P \rightarrow \sim Q$</p> | <p>$\sim P \rightarrow \sim Q$</p> | <p>If <u>an animal is not a dog</u>, then <u>it is not a mammal</u>. $\sim P$ $\sim Q$ False invalid "If not P, then not Q."</p> |
| <p>CONTRAPOSITIVE</p> | <p>The contrapositive of a conditional statement is formed by <u>negating both the hypothesis and the conclusion.</u> the converse. $Q \rightarrow P$</p> | <p>$\sim Q \rightarrow \sim P$</p> | <p>If <u>an animal is not a mammal</u>, then <u>it is not a dog</u>. $\sim Q$ $\sim P$ True valid</p> |

| | | | |
|-------------------------|--|--------------------------|--|
| EQUIVALENT STATEMENTS | Equivalent statements are two statements that are both true or both false. | | |
| PERPENDICULAR LINES | <p>If two lines that intersect to form a <u>right</u> angle, then they are perpendicular lines.</p> <p>If two lines are perpendicular lines, then they intersect to form <u>right</u> angles.</p> | \perp Perpendicular | <p>If  , then line a \perp line b.</p> <p>If line a \perp line b, then .</p> |
| BICONDITIONAL STATEMENT | <p>A statement that contains the phrase "if and only if."</p> <p>Both the conditional ($P \rightarrow Q$)</p> | $P \leftrightarrow Q$ | <p><u>Two lines intersect to form right angles,</u> if and only if <u>they are perpendicular lines.</u></p> <p> \leftrightarrow line a \perp line b.</p> <p>"P if and only if Q."</p> |

and the converse ($Q \rightarrow P$)
 must be true (equivalent statements)
 to write a biconditional ($P \leftrightarrow Q$)
 or $Q \leftrightarrow P$

conditional statement
if - then form

converse

$$Q \rightarrow P$$

inverse

$$\sim P \rightarrow \sim Q$$

contrapositive

$$\sim Q \rightarrow \sim P$$

biconditional

$$P \leftrightarrow Q$$

$$P \rightarrow Q$$